

CS380: Modern Functional Programming
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Types in Math

Consider the definitions below. Which of the mathematical phrases make sense?

$$\begin{array}{ll} x_1 = 5 & x_2 = -3 \\ z_1 = 3 + 4i & z_2 = 2 - i \\ A_1 = \{1, 2, 3\} & A_2 = \{8\} \\ f_1(x) = x^2 + 7 & f_2(x) = |x| \\ g_1(x, y) = x - y^2 & g_2(x, y) = xy \end{array}$$

$$M = [2 \ 3 \ 5 \ 7 \ 11]$$

$$N = \begin{bmatrix} 3 \\ 1 \\ 4 \\ 1 \\ 5 \end{bmatrix}$$

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|---|---------------------|
| 1. $x_1 + x_2$ | 14. $g_2 \circ g_1$ |
| 2. $x_1 + z_2$ | 15. $x_1 > x_2$ |
| 3. $x_1 + A_1$ | 16. $z_1 > z_2$ |
| 4. $f_1(x_2)$ | 17. $ x_1 $ |
| 5. $f_2(z_1)$ | 18. $ z_1 $ |
| 6. $g_1(x_1)$ | 19. $ A_1 $ |
| 7. $x_2 M$ | 20. $ f_1 $ |
| 8. $x_2 \in A_1$ | 21. $ M $ |
| 9. $A_1 \in x_2$ | 22. MN |
| 10. $f_1(f_2(x_1))$ | 23. NM |
| 11. $f_2 \circ f_1$ (where \circ is function composition) | 24. $g_2(M, N)$ |
| 12. $g_1(x_1, x_2)$ | 25. $ MN $ |
| 13. $g_2(z_1, z_2)$ | 26. $ NM $ |