Information Retrieval – Part 2

Deepak Kumar

Borges' *Library of Babel*

"…each book contains four hundred ten pages; each page, forty lines; each line, approximately eighty black letters. There are also letters on the front cover of each book; these letters neither indicate nor prefigure what the pages inside will say."
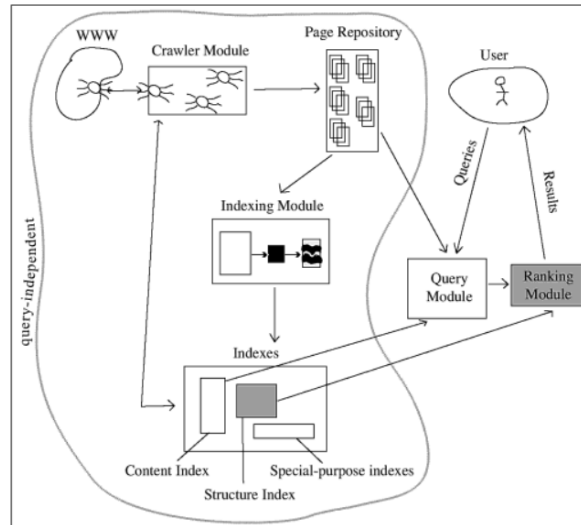
Q: How many books are in the library?
Q. How would you find what you're looking for?

Elements of a Search Engine

Web Information Retrieval

- Search Engines
- Queries
  phrase queries
  structure queries (NEAR, intitle:, …)
- Matching
- Inverted Index
  page number
  location
- Ranking & Relevance
- Metadata

Web Information Retrieval

- Search Engines
- Queries
  phrase queries
  structure queries
- Matching
- Inverted Index
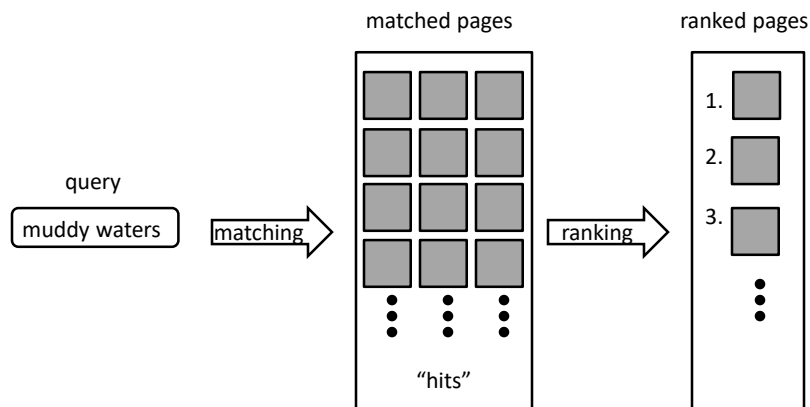 page number
  location
- Ranking & Relevance
- Metadata

**Efficient matching
is only one half the story.**

**The other grand challenge
is how to _rank_ the
matching pages**

5

Matching & Ranking

matched pages   ranked pages

query

muddy waters → matching → [hits] → ranking → 1. 2. 3.

"hits"

6

Ranking & Relevance

1
By far the most common cause of malaria is being bitten by an infected mosquito, but there are also other ways to contract the disease.

2
Our cause was not helped by the poor health of the troops, many of whom were suffering from malaria and other tropical diseases.

query

malaria cause

also	1-19	
...		
cause	1-6	2-2
...		
malaria	1-8	2-19
...		
whom	2-15	

Nearness can resolve the ranking!

Metadata
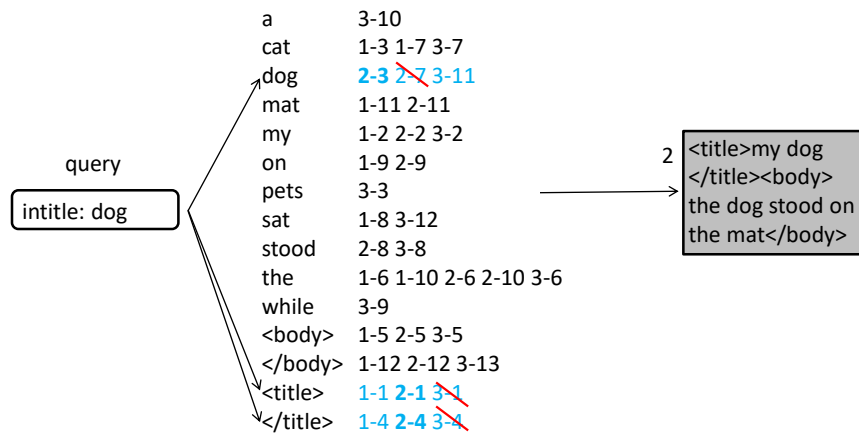
1
<title>my cat </title> <body> the cat sat on the mat </body>

2
<title>my dog </title><body> the dog stood on the mat</body>

3
<title>my pets </title><body>the cat stood while a dog sat

a	3-10
cat	1-3 1-7 3-7
dog	2-3 2-7 3-11
mat	1-11 2-11
my	1-2 2-2 3-2
on	1-9 2-9
pets	3-3
sat	1-8 3-12
stood	2-8 3-8
the	1-6 1-10 2-6 2-10 3-6
while	3-9
<body>	1-5 2-5 3-5
</body>	1-12 2-12 3-13
<title>	1-1 2-1 3-1
</title>	1-4 2-4 3-4

Structure Queries

a	3-10
cat	1-3 1-7 3-7
dog	**2-3** 2-7 3-11
mat	1-11 2-11
my	1-2 2-2 3-2
on	1-9 2-9
pets	3-3
sat	1-8 3-12
stood	2-8 3-8
the	1-6 1-10 2-6 2-10 3-6
while	3-9
\<body\>	1-5 2-5 3-5
\</body\>	1-12 2-12 3-13
\<title\>	1-1 **2-1** 3-1
\</title\>	1-4 **2-4** 3-4

query

intitle: dog

2 \<title\>my dog \</title\>\<body\> the dog stood on the mat\</body\>

Exploiting Link Structure

- ***PageRank*** exploits the structure of the web:

  Use of Hyperlinks to
  - count # of incoming links
  - Identifying web authority

- Use the above in determining ranking & relevance.

The Garage

Garage at 232 Santa Margarita, Menlo Park, CA

Google 1.0 (1998)

2-proc Pentium II 300mhz, 512mb, five 9gb drives
2-proc Pentium II 300mhz, 512mb, four 9gb drives
4-proc PPC 604 333mhz, 512mb, eight 9gb drives
2-proc UltraSparc II 200mhz, 256mb, three 9gb
drives, six 4gb drives
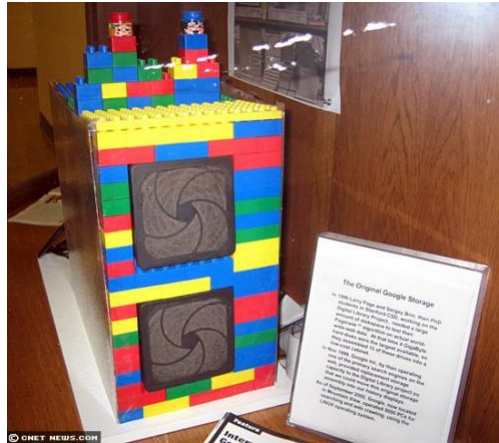Disk expansion, eight 9gb drives
Disk expansion, ten 9gb drives

That's a total of:
1792 megabytes of memory
366 gigabytes of disk storage
2933 megahertz in **10** CPUs

The Disk Storage

13

Google 1.0 (1998)

14

7

Hyperlinks

Ernie's Scrambled Eggs Recipe
Mix four eggs in a bowl with a little salt and pepper, …

Bert's Scrambled Eggs Recipe
First melt a tablespoon of butter, …

Ernie's recipe is good.

I really enjoyed Bert's recipe.

Bert's recipe is wonderful!

Bert's recipe is fantastic!

15

Hyperlinks: # Incoming Links

ranked higher based on #incoming links

Ernie's Scrambled Eggs Recipe
Mix four eggs in a bowl with a little salt and pepper, …

Bert's Scrambled Eggs Recipe
First melt a tablespoon of butter, …

Ernie's recipe is good.

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Bert's recipe is wonderful!

Bert's recipe is fantastic!

16

8

Hyperlinks: # Incoming Links

ranked higher based on #incoming links

Ernie's Scrambled Eggs Recipe
Mix four eggs in a bowl with a little salt and pepper, …

Bert's Scrambled Eggs Recipe
First melt a tablespoon of butter, …

Ernie's recipe is good.

I did not enjoy Bert's recipe.

Bert's recipe did not work.

Bert's recipe is unhealthy!

11/6/2019

17

Hyperlinks: Authority

Ernie's Scrambled Eggs Recipe
Mix four eggs in a bowl with a little salt and pepper, …

Bert's Scrambled Eggs Recipe
First melt a tablespoon of butter, …

Deepak Kumar's Home Page
I tried Ernie's recipe once, and its not bad at all.

Alton Brown's Home Page
Bert's recipe is clearly one of the best.

11/6/2019

18

9

Hyperlinks: Authority

Ernie's Scrambled Eggs Recipe
Mix four eggs in a bowl with a little salt and pepper, … ②

Bert's Scrambled Eggs Recipe
First melt a tablespoon of butter, … ⑩⓪

Deepak Kumar's Home Page
I tried Ernie's recipe once, and its not bad at all. ②

Alton Brown's Home Page
Bert's recipe is clearly one of the best. ⑩⓪

① ① ① ①

…100 pages…

① ① ① ①

①

①

Cycles

A B
C D E

Computing Authority Scores

Computing Authority Scores

Computing Authority Scores

Computing Authority Scores
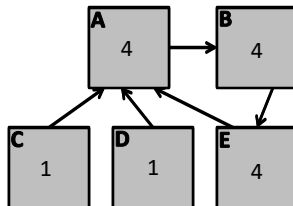
Computing Authority Scores

Computing Authority Scores

Computing Authority Scores

Computing Authority Scores

Computing Authority Scores

and so on…stuck in an infinite loop….

Sinks

dangling node

Sinks

The Random Surfer

restart probability = 15%

The Random Surfer

B

109

74

55

55

32

58

16

C

13

46

17

21

15

101

A
118

126

| 144 | **D**
|---|

after 1000 page visits

11/6/2019

33

The Random Surfer

B

10%

7%

4%

4%

4%

5%

2%

C

2%

4%

2%

2%

2%

10%

A
13%

14%

| 15% | **D**
|---|

after 1 million page visits
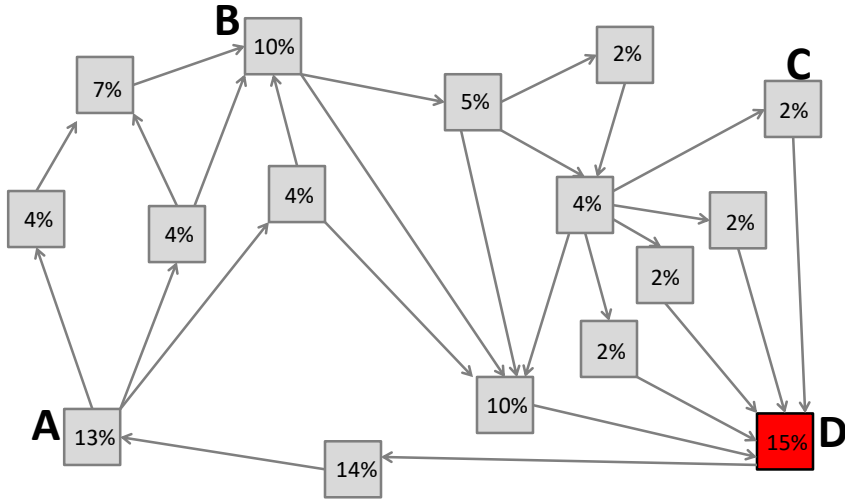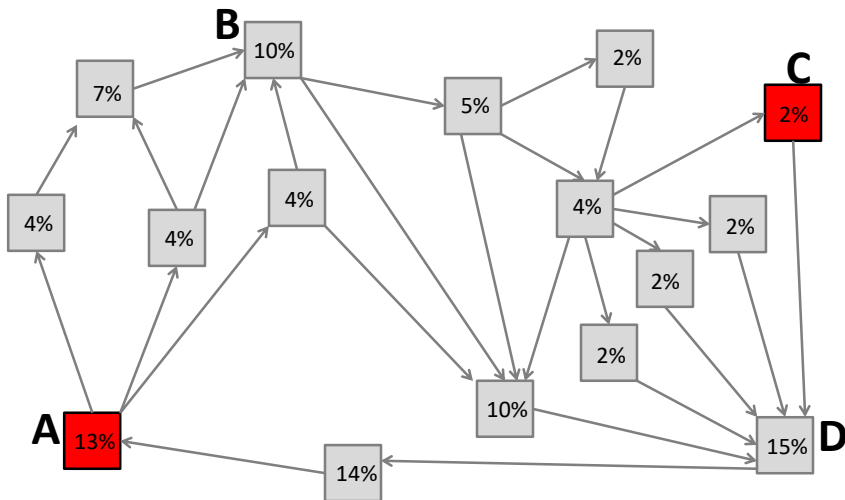
11/6/2019

34

17

The Random Surfer
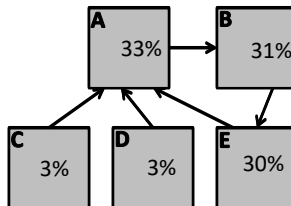
pages with many incoming links get high ranking

The Random Surfer

authoritative score

The Random Surfer

#links+authoritative score

37

The Random Surfer

Ernie's Scrambled Eggs Recipe
Mix four eggs in a bowl with a little salt and pepper, …
1%

Bert's Scrambled Eggs Recipe
First melt a tablespoon of butter, …
28%

0.4%

Deepak Kumar's Home Page
I tried Ernie's recipe once, and its not bad at all.
1%

0.4%

Alton Brown's Home Page
Bert's recipe is clearly one of the best.
32%

…100 pages…

0.4%

38

19

The Random Surfer

Formalizing PageRank

- Given a web page, P_i
- Set of pages pointing into P_i, B_{P_i}
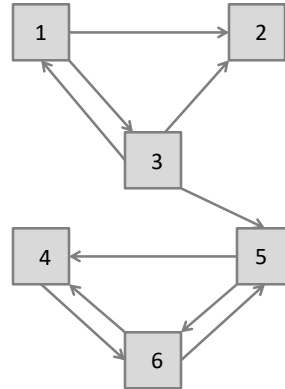- Number of outgoing links from page P_j, $|P_j|$
- PageRank of a page, $r(P_i)$

$$r(P_i) = \sum_{P_j \in B_{P_i}} \frac{r(P_j)}{|P_j|}$$

Computing PageRank

- $r(P_1) = r(P_3)$

- But, $r(P_3)$ is unknown

- To start, assume all pages
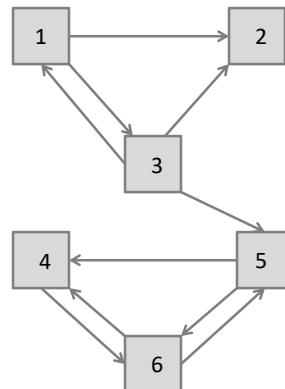 have rank $\frac{1}{n}$ $(n = 6)$

- $\therefore r(P_1) = \frac{1}{6}$

Computing PageRank

$r_0(P_1) = 1/6$
$r_0(P_2) = 1/6$
$r_0(P_3) = 1/6$
$r_0(P_4) = 1/6$
$r_0(P_5) = 1/6$
$r_0(P_6) = 1/6$

Computing PageRank

$r_1(P_1) = 1/18$
$r_1(P_2) = 5/36$
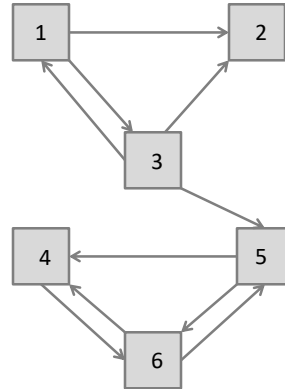$r_1(P_3) = 1/12$
$r_1(P_4) = 1/4$
$r_1(P_5) = 5/36$
$r_1(P_6) = 1/6$

$$r_{k+1}(P_i) = \sum_{P_j \in B_{P_i}} \frac{r_k(P_j)}{|P_j|}$$
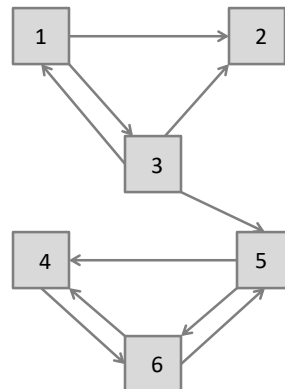
Computing PageRank

$r_2(P_1) = 1/36$
$r_2(P_2) = 1/18$
$r_2(P_3) = 1/36$
$r_2(P_4) = 17/72$
$r_2(P_5) = 11/72$
$r_2(P_6) = 14/72$

$$r_{k+1}(P_i) = \sum_{P_j \in B_{P_i}} \frac{r_k(P_j)}{|P_j|}$$

Computing PageRank

$r_2(P_1) = 1/36$ 5
$r_2(P_2) = 1/18$ 4
$r_2(P_3) = 1/36$ 5
$r_2(P_4) = 17/72$ 1
$r_2(P_5) = 11/72$ 3
$r_2(P_6) = 14/72$ 2

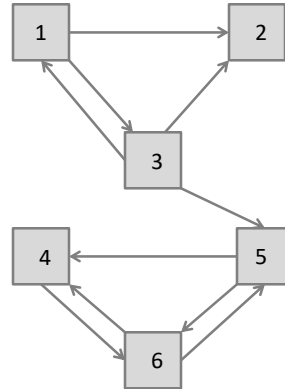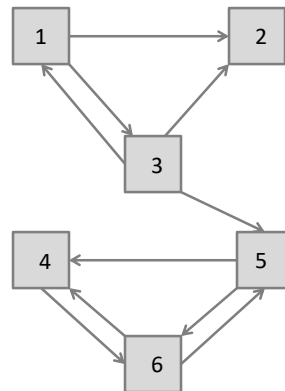$$r_{k+1}(P_i) = \sum_{P_j \in B_{P_i}} \frac{r_k(P_j)}{|P_j|}$$

Matrix Representation

- Adjacency Matrix

$$A = \begin{array}{c} \\ 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \end{array} \begin{array}{cccccc} 1 & 2 & 3 & 4 & 5 & 6 \\ \begin{bmatrix} 0 & 1 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 1 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 & 0 \end{bmatrix} \end{array}$$
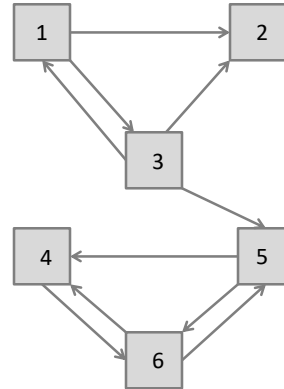
Matrix Representation

- Hyperlink Matrix, H

$$\begin{array}{c} \\ 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \end{array} \begin{array}{cccccc} 1 & 2 & 3 & 4 & 5 & 6 \\ \left[\begin{array}{cccccc} 0 & 1/2 & 1/2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 1/3 & 1/3 & 0 & 0 & 1/3 & 0 \\ 0 & 0 & 0 & 0 & 1/2 & 1/2 \\ 0 & 0 & 0 & 1/2 & 0 & 1/2 \\ 0 & 0 & 0 & 1 & 0 & 0 \end{array}\right] \end{array}$$

- $\pi_{k+1}{}^T = \pi_k{}^T H$

 where $\pi_k{}^T$ is the kth PageRank vector

The PageRank Equation

- $\pi^T = \pi^T(\alpha S + (1 - \alpha)E)$

where
S is the stochastic H matrix
E is the teleportation matrix
α is the scaling parameter

- Certain stochastic conditions apply!

Google Data Center

References

- *Google's PageRank and Beyond*, Amy N. Langville and Carl D. Meyer, Princeton University Press, 2006.
- *Nine Algorithms That Changed The Future*, John MacCormick, Princeton University Press, 2012.
- *The Unimaginable Mathematics of Borges' Library of Babel*, William G. Bloch, Oxford University Press, 2008.