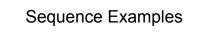
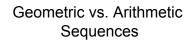


- A sequence is a function whose domain is a subset of *Z*
 - Usually from the positive or non-negative integers
 - can be infinite
- *a_n* is a term in the sequence
- $\{a_n\}$ means the entire sequence



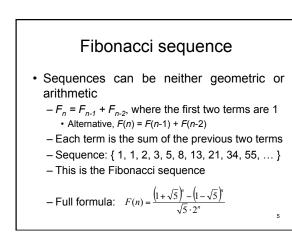
- a_n = 3n
 The terms in the sequence are a₁, a₂, a₃, ...
- The sequence $\{a_n\}$ is $\{3, 6, 9, 12, ...\}$
- $b_n = 2^n$
 - The terms in the sequence are b_1 , b_2 , b_3 , ... - The sequence $\{b_n\}$ is $\{2, 4, 8, 16, 32, ...\}$
- Sequences are indexed from 1 – Not in all textbooks, though!

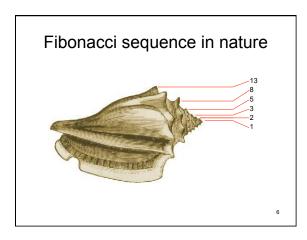


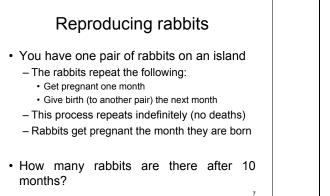
- The difference is in how they grow
- Arithmetic sequences increase by a constant *amount*
 - $-a_n = 3n$: { 3, 6, 9, 12, ... }
 - Each number is 3 more than the previous
 - Of the form: f(x) = dx + a
- Geometric sequences increase by a constant factor
 - $-b_n = 2^n$: { 2, 4, 8, 16, 32, ... }
 - Each number is twice the previous - Of the form: $f(x) = ar^x$



2

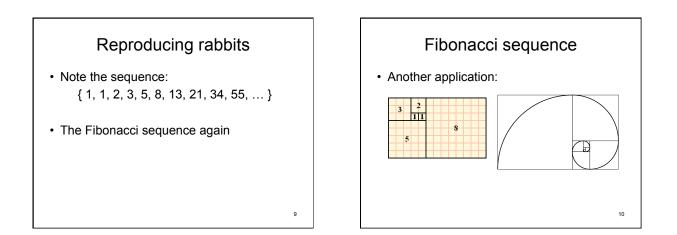


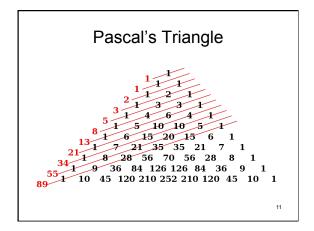


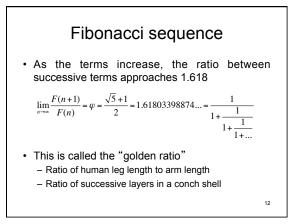


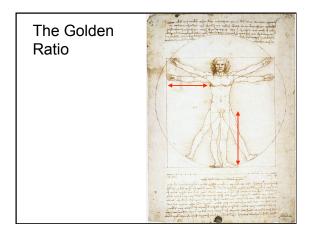
Reproducing rabbits First month: 1 pair The original pair Second month: 1 pair - The original (and now pregnant) pair Third month: 2 pairs The child pair (which is pregnant) and the parent pair (recovering) Fourth month: 3 pairs – "Grandchildren": Children from the baby pair (now pregnant) - Child pair (recovering) Parent pair (pregnant)

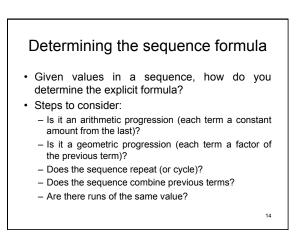
- Fifth month: 5 pairs
- Both the grandchildren and the parents reproduced - 3 pairs are pregnant (child and the two new born rabbit pairs)

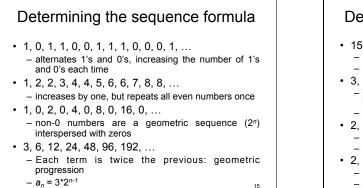




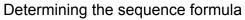








15



- 15, 8, 1, -6, -13, -20, -27, ... - Each term is 7 less than the previous term $-a_n = 22 - 7n$
- 3, 5, 8, 12, 17, 23, 30, 38, 47, ... - The difference between successive terms increases by one each time: $a_1 = 3$, $a_n = a_{n-1} + n$ $-a_n = n(n+1)/2 + 2$
- 2, 16, 54, 128, 250, 432, 686, ... - Each term is twice the cube of n $-a_n = 2^* n^3$
- 2, 3, 7, 25, 121, 721, 5041, 40321 - Each successive term is about *n* times the previous $-a_n = n! + 1$

