

# Quicker Quicksort

## Sorting Stability

## Hashing and Maps

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# MergeSort & QuickSort

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- Inefficient on small lists
  - lots of recursive calls (on very small pieces) eat time
- Idea:
  - Rather than make recursive calls down to size 1 cut off recursion earlier and use insertion sort

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# Hybrid MergeSort

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put insertion sort into the base case and make the base case bigger

```
private void doMergeSort3i(int lowerIndex, int higherIndex) {  
    if (lowerIndex > (higherIndex-12)) {  
        iSort.insertionSortIP(array, lowerIndex, higherIndex);  
    } else if (lowerIndex < higherIndex) {  
        int middle = lowerIndex + (higherIndex - lowerIndex) / 2;  
        // Below step sorts the left side of the array  
        doMergeSort3i(lowerIndex, middle);  
        // Below step sorts the right side of the array  
        doMergeSort3i(middle + 1, higherIndex);  
        // Now merge both sides  
        mergeParts3(lowerIndex, middle, higherIndex);  
    }  
}
```

Empirically, 10-15  
works best

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# Hybrid Quicksort

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For quicksort, it is quicker to cut off early (as with mergesort) but run insertion sort once on at the end.

```
public int[] qs4i(int inputArr[]) {
    doQS4i(inputArr, 0, inputArr.length-1);
    new Insertion().insertionSort2(inputArr);
    return inputArr;
}

private void doQS4i(int arr[], int begin, int end)
{
    if ((end-begin) < 15 ) {
        // just let it drop
    } else {
        int partitionIndex = partition(arr, begin, end);
        doQS4i(arr, begin, partitionIndex-1);
        doQS4i(arr, partitionIndex+1, end);
    }
}
```

Empirically, 10-15  
works best

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# Stability

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- Suppose you have multiple things on which to sort. Eg spreadsheet columns
  - Ties in column B should be sorted by column A
- Can do this with two sorting passes if the sort is “stable”.
- Mergesort is stable
- Quicksort is not

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# The student class

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- Comparators for name and age
- Static methods
  - Are not always evil
    - Are reasonable when the return value of the method is dependent ONLY on arguments to the method
    - Should be used carefully!!!!!!!!!!!!
- switch to VSC for student, mergeOb and qOb

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# Map

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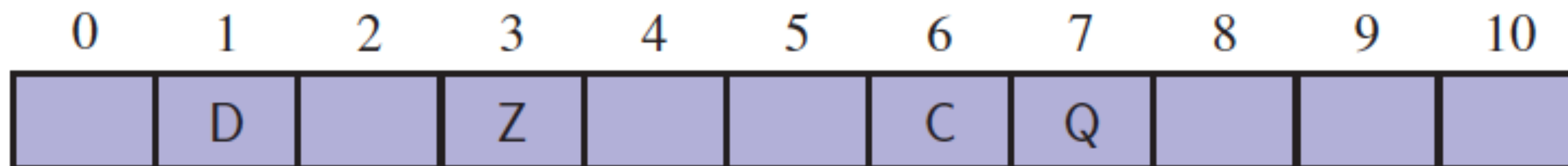
- A searchable collection of key-value pairs
- Multiple entries with the same key are not allowed
- Also known as dictionary (python), associative array (perl)

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# Notion of a Map

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- Intuitively, a map  $M$  supports the abstraction of using keys as indices with a syntax such as  $M[k]$ .
- Simplest setting is a map with  $n$  items using keys that are known to be integers from  $0$  to  $N-1$ , for some  $N \geq n$ .





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# Improving Maps

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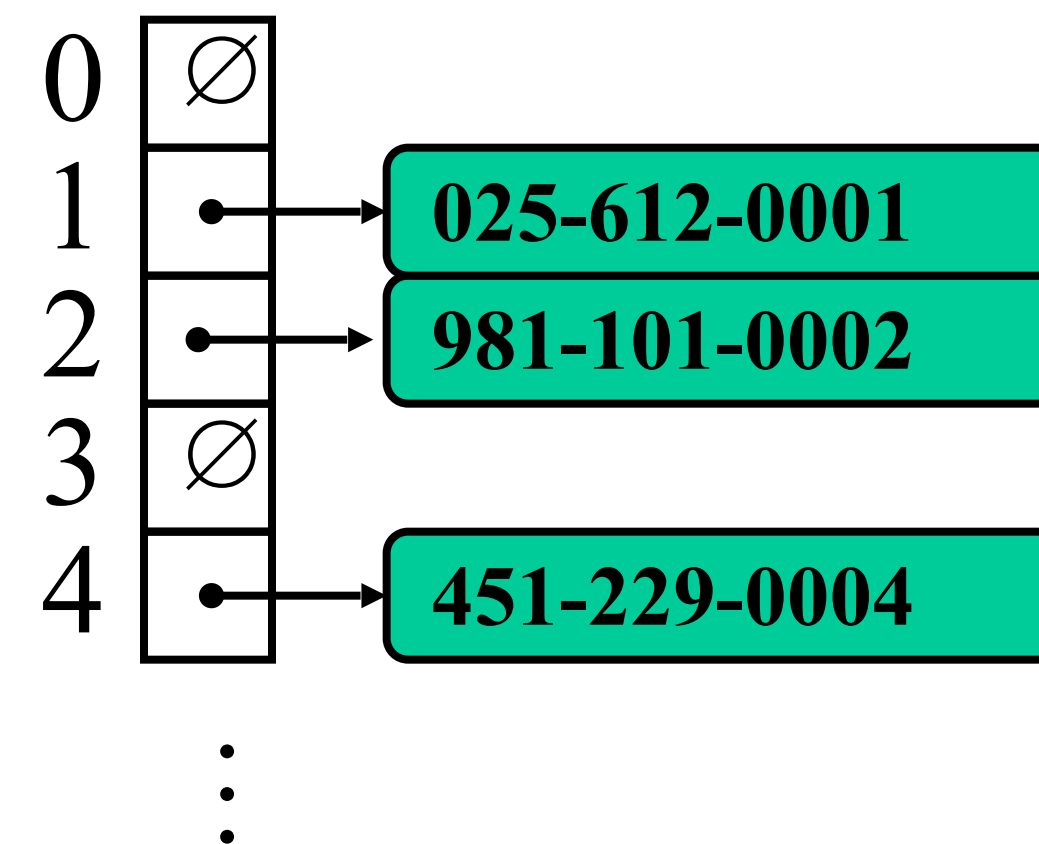
- Can we tradeoff time and space
  - UnsortedMap implementation
    - efficient spacewise
    - not great timewise
    - So if storing lots of info but accessing rarely, OK
  - But what if storing less and access often?
  - Can we get  $O(1)$  time for get/set/remove at a cost of space?

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# More General Keys

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- Earlier: motivated Maps with discussion of keys as integers. What if our keys are not integers in range  $0$  to  $N-1$ ?
- Use a function to map keys to integers into the right range
- Example: Rather than entire SSN, use only last 4 digits



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# Hash Functions and Tables

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- A hash function  $h$  maps a key to integers in a fixed interval  $[0, N - 1]$
- $h(x) = x \% N$  is such a function for integers
- A hash table is an array of size  $N$ 
  - associated hash function  $h$
  - item  $(k, v)$  is stored at index  $h(k)$

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# Java Hash classes

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- HashMap & Hashtable
  - HashMap is quicker (25% in my tests)
  - HashMap is NOT thread safe
- takes a key - value pair (a la priority queue)
  - applies a hash function to the key and stores the object
  - You do not know the hash function
- $O(1)$  time for store and access

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# Mini-Homework (part 1)

## What is the output of main?

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// Using the same student class as earlier in lecture

```
public static void main(String args[])
{
    HashMap<Integer, Student> hm=new HashMap<>();
    for (Student st : Student.getStudents())
        hm.put(st.getYear(), st);
    for (Map.Entry m:hm.entrySet()) {
        System.out.println(m.getKey()+"--"+m.getValue());
    }
}
```

```
public class Student {
    public static Student[] getStudents()
    {
        Student[] sss = new Student[12];
        sss[0]=new Student("Lisa", 23);
        sss[1]=new Student("Rosie", 22);
        sss[2]=new Student("Charlotte", 22);
        sss[3]=new Student("Synthia", 20);
        sss[4]=new Student("AnnaSophia", 23);
        sss[5]=new Student("Flora", 21);
        sss[6]=new Student("Libby", 21);
        sss[7]=new Student("Rachel", 22);
        sss[8]=new Student("Catherine", 23);
        sss[9]=new Student("Erin", 22);
        sss[10]=new Student("Xinran", 23);
        sss[11]=new Student("Ashley", 23);
        return sss;
    }
}
```

# Mini Homework (part 2)

## insertion sort for quicksort

1,2,3,4,5,6,9,7,8,10,11,14,13,12,15,16,17,18,19,22,20,21,25,24,22,23

For the data above, how many compare and move operations are required to sort using insertion sort. If the “average” case time for insertion sort is  $n^2/4$  how much faster is it in this, mostly sorted, case