

# Trees

Part 4

March 31

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# Insert

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```
public void insert(E element) {  
    root = iInsert(root, element);  
}
```

```
private Node iInsert(Node treepart, E element) {  
    if (treepart == null) {  
        size++;  
        return new Node(element);  
    }  
    int cmp = treepart.payload.compareTo(element);  
    if (cmp==0) return treepart;  
    if (cmp>0) {  
        treepart.left = iInsert(treepart.left, element);  
        return treepart;  
    }  
    else {  
        treepart.right = iInsert(treepart.right, element);  
        return treepart;  
    }  
}
```

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# Remove

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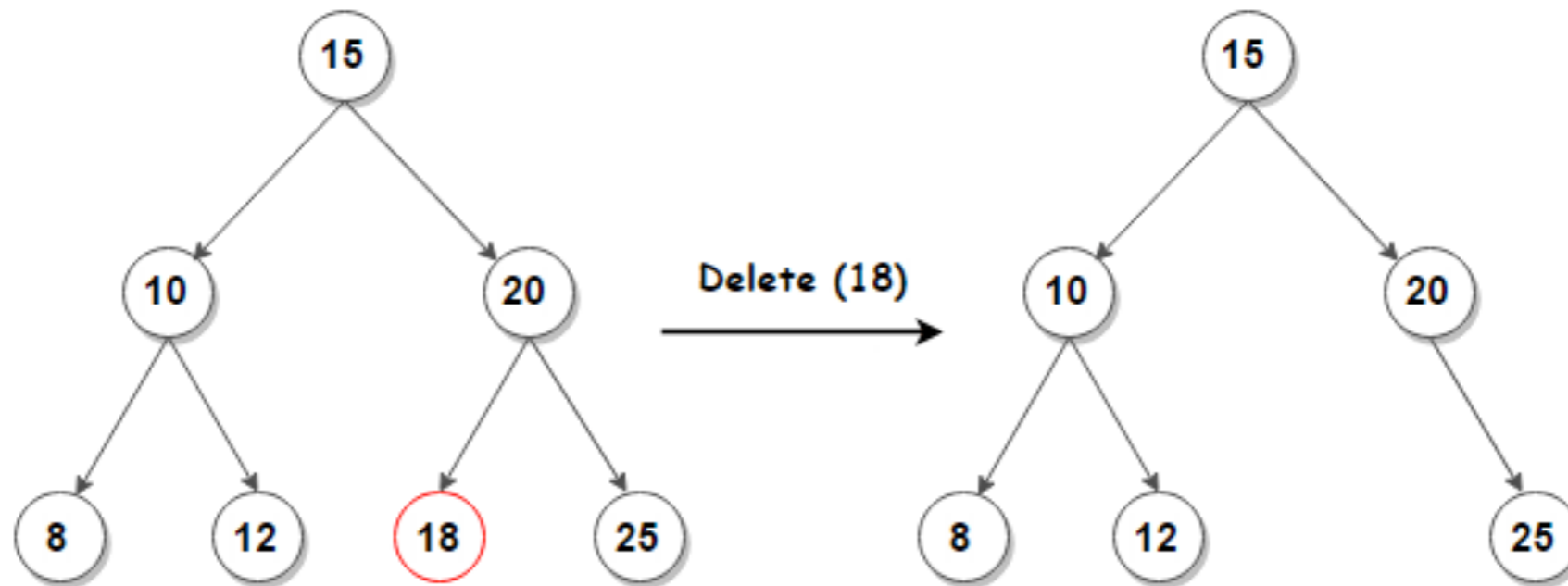
- `boolean remove(E element);`
- returns true if element existed and was removed and false otherwise
- Cases
  1. element not in tree
  2. element is a leaf
  3. element has one child
  4. element has two children

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# No children (Leaf)

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- Just delete

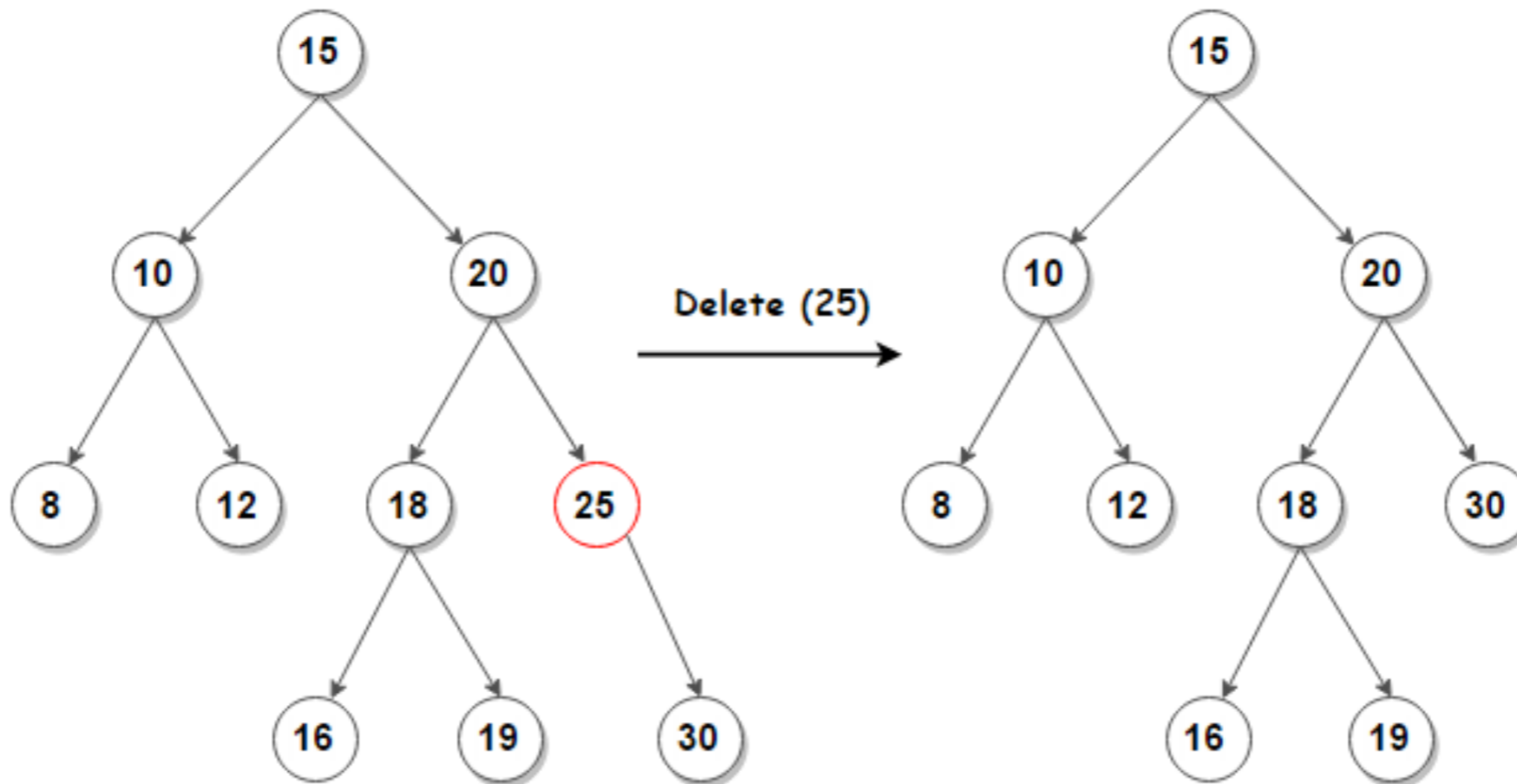


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# One child

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- Replace with child – skip over like in linked list

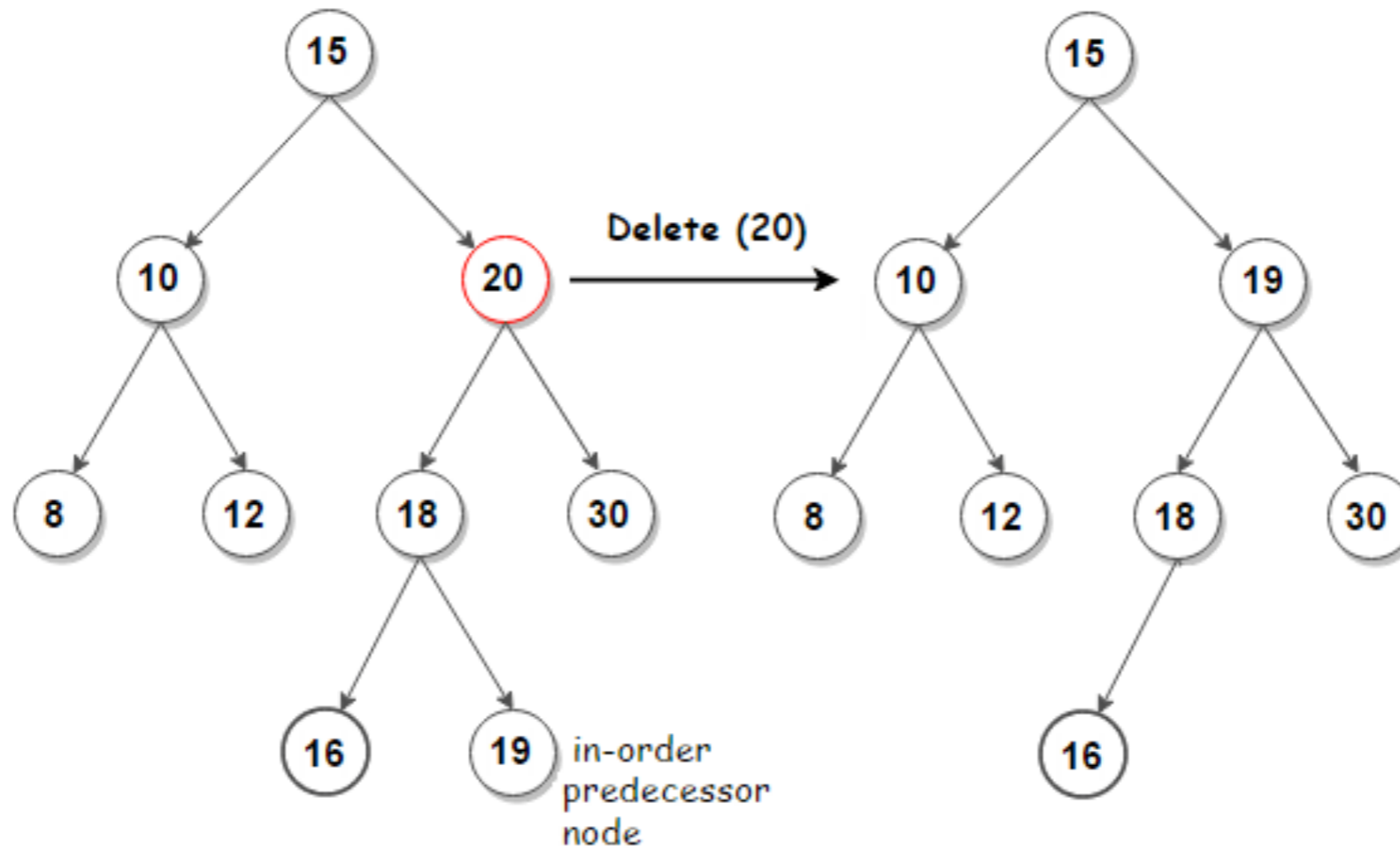


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# 2 children

## Replace with Predecessor

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# Getting the predecessor

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- Pseudocode:
  - Go left
    - repeat
      - go right
      - until right child is null

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# Getting the Max

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```
// E pred = iMaxPayload(treepart.left);
```

```
private E iMaxPayload(Node treepart) {  
    if (treepart.right==null)  
        return treepart.payload;  
    else  
        return iMaxKey(treepart.right);  
}
```

**Recursive**

```
private E iMaxPayloadNR(Node treepart) {  
    Node rightChild = treepart.right;  
    while (rightChild !=null) {  
        treepart = rightChild;  
        rightChild = treepart.right;  
    }  
    return treepart.payload;  
}
```

**Non-Recursive**



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# Remove

## Stepping down the tree

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```
public boolean removeAlt(E element) {  
    if (root==null)  
        return false;  
    return iRemoveAlt(root, null, element);  
}
```

```
private boolean iRemoveAlt(Node treepart, Node parent,  
                            E toBeRemoved) {  
    int cmp = treepart.payload.compareTo(toBeRemoved);  
    if (cmp>0) {  
        if (treepart.left==null) return false; // case 1  
        return iRemoveAlt(treepart.left, treepart, toBeRemoved);  
    } else if (cmp<0) {  
        if (treepart.right==null) return false; // case 1  
        return iRemoveAlt(treepart.right, treepart, toBeRemoved);  
    }  
    ...  
}
```

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# Remove

## Case 2: no children

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```
} else { // cmp==0
    // this is the thing I want to get rid of!!!!
    if (treepart.left==null && treepart.right==null) {
        // Case 1: no children
        if (parent==null) {
            root=null;
        } else {
            if (parent.right==treepart)
                parent.right=null;
            else
                parent.left=null;
        }
        size--;
        return true;
    }
}
```

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# Remove

## Case 3: 1 child

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```
if (treepart.left==null) {  
    // the right branch is NOT null  
    // Case 2: Only a right child  
    if (parent==null) {  
        root=treepart.right;  
    } else {  
        if (parent.right==treepart)  
            parent.right = treepart.right;  
        else  
            parent.left = treepart.right;  
    }  
    size--;  
    return true;  
}
```

**Code for only left child is essentially identical**

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# Remove

## Case 4: 2 children

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```
// case 4: Two children  
E pred = iMinKey(treepart.right);  
iRemoveAlt(treepart.right, treepart, pred);  
treepart.payload = pred;  
return true;
```

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# Mini-homework

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- On class website open `LinkedBinaryTree` code for today's lecture.
- Find the `remove` method.
  - Not `removeAlt` which I just discussed, `remove`
- Build a tree with the following data:
  - 154, 181, 85, 99, 118, 57, 116, 190, 135, 174, 80, 43, 86, 42, 70, 183, 50, 149, 82, 130
- Write a detailed trace through all method calls and the call stack for the deletion of 99 followed by the deletion of 154.
  - Along the lines of insert at the beginning of class today.
  - For another example, see lecture notes from March 3 <https://cs.brynmawr.edu/Courses/cs206/spring2020/lec12/lec12.pdf>
  - Feel free to use VSC breakpoints to help you, or just do it by hand