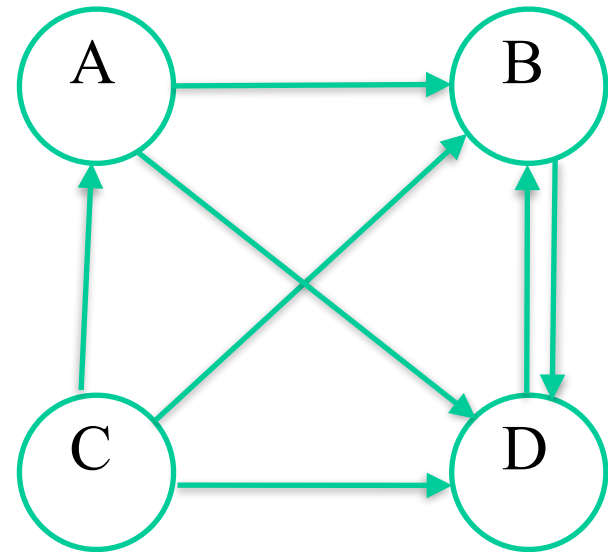

Graphs

Graphs

- Consist of nodes and edges
 - edges may be
 - weighted or unweighted
 - Directed or undirected
- No distinguished starting location
- Loops allowed



A graph with 4 nodes and unweighted, directed edges

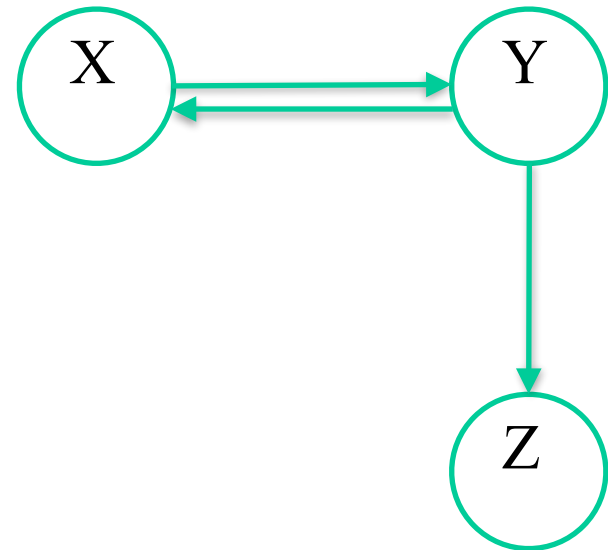
Adjacency Lists

- Each node holds list of edges leaving the node
 - Add an ArrayList of edges to the node definition
- Edge need only store destination
- How do you store bi-directional links?

```
private class Node<H> {  
    // Node content  
    public H payload;  
    // hold the list  
    public ArrayList<Edge<G>> edges;  
  
    public Node(H payl) {  
        this.payload = payl;  
        this.edges = new ArrayList<Edge<G>>();  
    }  
  
    public void addEdge(Node<G> n, double w) {  
        edges.add(new Edge<G>(n, w));  
    }  
}
```

Graph Navigation

- Can I get from Node X to Node Z?
 - Adj List representation?



Path Exists

```
boolean pathExists(Starting, ending)
  Stack s ← new Stack
  add starting point to stack
  while stack not empty
    n ← pop stack
    if n is destination
      return true
    With each edge from n
      add end to stack
  return false
```

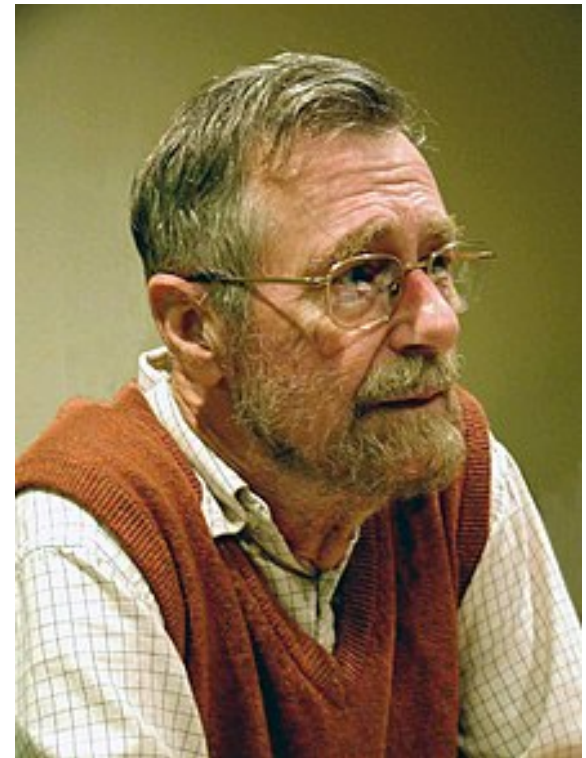
- Problem: loops
 - How to handle?
- A “depth first” traversal

Shortest unweighted path

- Change path exists to from stack to Queue
 - need to store paths

Shortest Weighted Path

- Edsger W. Dijkstra
- “Dijkstra’s shortest path algorithm” (1956)
- non-negative weights
- A “greedy” algorithm
 - Do the best thing you can based on local info and hope you get a global best.



1930-2002

PhD in CS (1959)

Pioneered structured programming

Seminal work in distributed computing

Curmudgeon

Finding Groups

- Suppose undirected links
- Question: Identify groups
 - A group is all the nodes in a graph that can be reached each other
- How does this problem change when you have directed links?