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# Dictionaries Hash Tables

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# Java Inner Classes

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- A class defined WITHIN another class
  - Cannot be public (so private or protected)
- Reason
  - Encapsulation!!!!
  - Class writer can change it as needed
  - group together data items
  - for example, key-value pairs

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# Inner classes

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- Are real classes
- Are usually very simple
- They can inherit from other external classes or other internal classes
- Variables are “public” to the containing class
  - they are only “public” to the containing class so no encapsulation violation
  - No need for get/set accessors
    - just use . accessors

# Inner class Example

```
public class OutCl {  
    private class InnCl {  
        private int value1;  
        private String value2;  
        public InnCl(int v1, String v2) {  
            this.value1 = v1;  
            this.value2 = v2;  
        }  
        @Override  
        public String toString() {  
            return value1 + " " + value2;  
        }  
    }  
}
```

INNER CLASS DEFINED ... NOTE IT IS PRIVATE

Inner class used .. just like any other class from within the class. However, cannot be used from static context, so cannot be used in Main

```
    public void worker() {  
        InnCl icl1 = new InnCl(1, "Bob");  
        InnCl icl2 = new InnCl(2, "Carol");  
        icl1.value1 = 3;  
        icl2.value2 = "Alice";  
        System.out.println(icl1 + "\n" + icl2);  
    }  
  
    public static void main(String[] args) {  
        OutCl ocl = new OutCl();  
        ocl.worker();  
    }  
}
```

# Generic Inner Class!

```
public class OutCLGen<R,S> {  
    /**  
     * The inner class, Generically  
     */  
    private class InnCl<Y,Z> {  
        private Y value1; // a value  
        private Z value2; // another value  
  
        public InnCl(Y v1, Z v2) {  
            this.value1 = v1;  
            this.value2 = v2;  
        }  
  
        public String toString() {  
            return value1 + " " + value2;  
        }  
    }  
}
```

Inner class has different generic parameters than its surrounding class. Realistically, they will almost always be the same, but this allows for difference

```
public void worker(R rValue, S sValue) {  
    InnCl<String, String> icl1 = new InnCl<>("Alice", "Bob");  
    InnCl<R,S> icl2 = new InnCl<>(rValue, sValue);  
    icl1.value1 = 3;  
    System.out.println(icl1 + "\n" + icl2);  
}  
  
public static void main(String[] args) {  
    OutCLGen<Integer, String> ocl = new OutCLGen<>();  
    ocl.worker(42, "Carol");  
}
```

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# Dictionary (Map)

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- A searchable collection of key-value pairs
  - A lot of this course will involve key value pairs
    - A lot of life is about key value pairs
      - SSN, tax history
      - BMID no, student record
    - .....
  - Multiple entries with the same key are not allowed
  - AKA associative array (perl)

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# What do you do with dictionaries (Physical)

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- Look up based on a key item (word)
  - to get definition
- Add items (word and definition)
- Remove Items (word)
- Others??

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# Map Interface

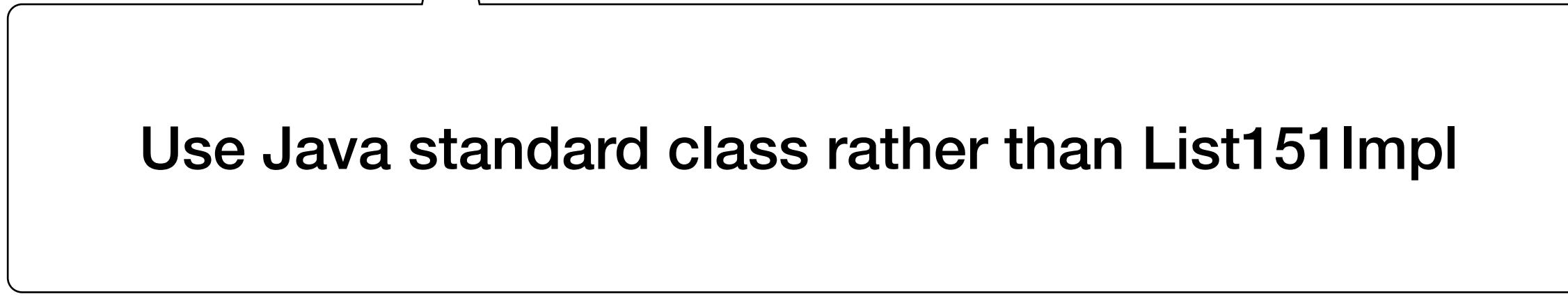
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- <https://docs.oracle.com/javase/7/docs/api/java/util/Map.html>

```
public interface Map151Interface<K, V> {  
    public void put(K key, V val);  
    public V get(K key);  
    public boolean containsKey(K key);  
    public int size();  
    public Set<K> keySet();  
}
```

# Map Implementation

```
public class Map151<K,V> implements Map151Interface<K,V>{  
    private ArrayList<Pair<K,V>> underlying = new ArrayList<>();  
  
    private class Pair<L,W> {  
        public L ky;  
        public W vl;  
        Pair(L key, W value) {  
            ky=key;  
            vl=value;  
        }  
        // if needed, override equals  
    }  
}
```



Use Java standard class rather than List151Impl

# Map Implementation (pt 2)

```
public boolean containsKey(K key) {  
    return null != getKV(key);  
}  
  
private Pair<K,V>getKV(K ky) {  
}  
  
    public void put(K key, V val) {  
        Pair<K,V> pair =getKV(key);  
        if (pair==null) {  
            Pair<K,V> np = new Pair<>(key, val);  
            underlying.add(np);  
        } else {  
            pair.value=val;  
        }  
    }  
  
    public V get(K key) {  
        Pair<K,V> pair = getKV(key);  
        if (pair!=null)  
            return pair.value;  
        return null;  
    }  
  
    /**  
     * The number of items in the map  
     * @return The number of items in the map  
     */  
    public int size() {  
        return underlying.size();  
    }
```

In the book's parlance, this is an unsorted, ArrayList-based dictionary.

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# Maps - time complexity

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- Put
  - need to search the existing items (`iContainsKey`)
  - so time to add 1 item in  $O(n)$
  - BUT if you are adding  $n$  items the you are doing an  $O(n)$  process  $n$  times so your time is  $O(n^2)$
- Get
  - similar analysis so  $O(n^2)$  to do  $n$  gets
  - So maps get slow when  $n$  gets large.

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# Using Maps to track stock positions

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- Suppose you are an active stock trader, buying and selling all the time.
- One challenge is simply keeping track of how much you have of what
- Further suppose,
  - you have a csv file
    - STOCK ID, AMT
    - Idea
    - Use ReadCSV and Map151 to track

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# StockTracker

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```
Map151<String, Integer> positions;

public StockTracker() {
    positions = new Map151<>();
}

public void track(String filename) {
    ArrayList<String[]> data = new ReadCSV().csvCollection(filename);
    System.out.println("trades read: " + data.size());
}

}
```

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# HashTables

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- A hash table is a form of a map that has better time complexity
- A hash table consists of
  - an array of size  $N$
  - an associated hash function  $h$  that maps keys to integers in  $[0, N-1]$ 
    - If keys are integers, then  $h(x) = x \% N$  is a hash function
  - pair  $(k, v)$  is stored at index  $h(k)$

# Simple Hashtable Implementation

```
public class SimpleHT {  
    private class Pair {  
        // the key. Once set it cannot be changed  
        public final Integer key;  
        // the value  
        public String value;  
        //Create a key value pair.  
        Pair(Integer ky, String val) {  
            key = ky;  
            value = val;  
        }  
    }  
  
    NO generics ... too simple  
  
    private Pair[] backingArray;  
    public SimpleHT() {  
        backingArray = new Pair[4];  
    }  
    private int h(int k) {  
        return k%4;  
    }  
    public void put(Integer key, String value) {  
        backingArray[h(key)] = new Pair(key, value);  
    }  
    public String get(Integer key) {  
        return backingArray[h(key)].value;  
    }  
}
```

4!!!???

# SimpleHT Example/Test

```
public static void main(String[] args) {
    SimpleHT sht = new SimpleHT();
    for (int i=0; i<10; i++) {
        System.out.println("adding
item with key=" + i + " value=" +
String.format("%c", 'a'+i));
        sht.put(i,
String.format("%c", 'a'+i));
    }
    for (int i=0; i<10; i++)
        System.out.println("getting
key="+i+ " value="+sht.get(i));
}
```

Two problems:

1. a poor hashing function.
2. Storing more than there is room for

adding item with key=0 value=a  
adding item with key=1 value=b  
adding item with key=2 value=c  
adding item with key=3 value=d  
adding item with key=4 value=e  
adding item with key=5 value=f  
adding item with key=6 value=g  
adding item with key=7 value=h  
adding item with key=8 value=i  
adding item with key=9 value=j  
getting key=0 value=i  
getting key=1 value=j  
getting key=2 value=g  
getting key=3 value=h  
getting key=4 value=i  
getting key=5 value=j  
getting key=6 value=g  
getting key=7 value=h  
getting key=8 value=i  
getting key=9 value=j

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# Hash Functions

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- The goal is to “disperse” the keys in an appropriately random way
  - A hash function is usually specified as the composition of two functions:
    - hash code: key  $\rightarrow$  integers
    - compression: integers  $\rightarrow$  [0, N-1]

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see SepChainHT.java

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# Hash Functions

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- Goals:
  - Minimize collisions
  - Quickly transform key to integer
- Common Approach for non-integer keys:
  - 1. Transform key into String
  - 2. Do something character-by-character on string

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# Char-by-char in String

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- String s = "abc";
  - `s.charAt(0) == 'a';`
  - `s.charAt(0) == 97;`
    - both are correct.
- Suppose Hash func is just add ASCII values of all chars in string.

Key	Char values	As integer
aba	97+98+97	292
baa	98+97+97	292
aab	97+97+98	292

# ASCII Table

dec	hex	oct	char	dec	hex	oct	char	dec	hex	oct	char	dec	hex	oct	char
0	0	000	NULL	32	20	040	space	64	40	100	@	96	60	140	`
1	1	001	SOH	33	21	041	!	65	41	101	A	97	61	141	a
2	2	002	STX	34	22	042	"	66	42	102	B	98	62	142	b
3	3	003	ETX	35	23	043	#	67	43	103	C	99	63	143	c
4	4	004	EOT	36	24	044	\$	68	44	104	D	100	64	144	d
5	5	005	ENQ	37	25	045	%	69	45	105	E	101	65	145	e
6	6	006	ACK	38	26	046	&	70	46	106	F	102	66	146	f
7	7	007	BEL	39	27	047	'	71	47	107	G	103	67	147	g
8	8	010	BS	40	28	050	(	72	48	110	H	104	68	150	h
9	9	011	TAB	41	29	051	)	73	49	111	I	105	69	151	i
10	a	012	LF	42	2a	052	*	74	4a	112	J	106	6a	152	j
11	b	013	VT	43	2b	053	+	75	4b	113	K	107	6b	153	k
12	c	014	FF	44	2c	054	,	76	4c	114	L	108	6c	154	l
13	d	015	CR	45	2d	055	-	77	4d	115	M	109	6d	155	m
14	e	016	SO	46	2e	056	.	78	4e	116	N	110	6e	156	n
15	f	017	SI	47	2f	057	/	79	4f	117	O	111	6f	157	o
16	10	020	DLE	48	30	060	0	80	50	120	P	112	70	160	p
17	11	021	DC1	49	31	061	1	81	51	121	Q	113	71	161	q
18	12	022	DC2	50	32	062	2	82	52	122	R	114	72	162	r
19	13	023	DC3	51	33	063	3	83	53	123	S	115	73	163	s
20	14	024	DC4	52	34	064	4	84	54	124	T	116	74	164	t
21	15	025	NAK	53	35	065	5	85	55	125	U	117	75	165	u
22	16	026	SYN	54	36	066	6	86	56	126	V	118	76	166	v
23	17	027	ETB	55	37	067	7	87	57	127	W	119	77	167	w
24	18	030	CAN	56	38	070	8	88	58	130	X	120	78	170	x
25	19	031	EM	57	39	071	9	89	59	131	Y	121	79	171	y
26	1a	032	SUB	58	3a	072	:	90	5a	132	Z	122	7a	172	z
27	1b	033	ESC	59	3b	073	;	91	5b	133	[	123	7b	173	{
28	1c	034	FS	60	3c	074	<	92	5c	134	\	124	7c	174	
29	1d	035	GS	61	3d	075	=	93	5d	135	]	125	7d	175	}
30	1e	036	RS	62	3e	076	>	94	5e	136	^	126	7e	176	~
31	1f	037	US	63	3f	077	?	95	5f	137	_	127	7f	177	DEL

www.alpharithms.com

# Horner's method: Convert any object to integer

Start with  
an object, then just call  
its `toString`

Almost any  
prime number

Handles really  
large numbers

```
public BigInteger objectHasher(Object ob) {  
    return stringHasher(ob, toString());  
}  
public BigInteger stringHasher(String ss) {  
    BigInteger mul = BigInteger.valueOf(23);  
    BigInteger ll = BigInteger.valueOf(0);  
    for (int i=0; i<ss.length(); i++) {  
        ll = ll.multiply(mul);  
        ll = ll.add(BigInteger.valueOf(ss.charAt(i)));  
    }  
    return ll;  
}
```

$33^{15} = 59938945498865420543457$

---

# Collisions

---

drawing 500 unique words from Oliver Twist and assuming a hashtable size of 1009, get these collisions

- 16 probable child when
- 42 fagins xxix importance that xv administering
- 104 stage pledge near
- 132 surgeon can night
- 271 things fang birth
- 341 alone sequel life
- 415 maylie check circumstances
- 418 mentioning containing growth
- 625 meet she first
- 732 there affording encounters
- 749 possible out acquainted
- 761 never xviii after goaded where
- 833 marks jew gentleman
- 985 adventures inseparable experience

---

# Collisions

---

- Handling of collisions is one of the most important topics for hash tables
  - Rehashing
    - make the table bigger
    - $O(n)$  time so want to avoid
    - Also, simply making table bigger does not always eliminate collisions
  - Alternative to rehashing
    - Separate Chaining
    - Probing

---

# Separate Chaining

---

- Idea: each spot in hashtable holds a list of key value pairs when the key maps to that hashvalue.
- Replace the item if the key is the same
- Otherwise, add to list
- Generally do not want more than about number of objects as size of table
- Chains can get long

---

# Hash tables get crowded, chains get long

---

HT\_SIZE=1009

Using unique words drawn from “Oliver Twist”.  
Unique count at top of table

278

0	762
1	217
2	29
3	1
4	0
5	0
6	0
7	0
8	0
9	0

473

0	622
1	308
2	73
3	5
4	1
5	0
6	0
7	0
8	0
9	0

1550

0	210
1	342
2	252
3	136
4	55
5	9
6	4
7	1
8	0
9	0

2510

0	87
1	198
2	268
3	208
4	140
5	70
6	26
7	10
8	2
9	0

---

# In class exercise

---

- Show the final contents of the hashtable using separate chaining assuming
  - table size is 7
  - $h(t) = t \% 7$
  - Data: <0,a> <32,b> <39,c> <12,d>  
<14,e> <35,f> <27,g> <13,h> <15,i>  
<5,j> <12,k> <13,l> <4,m> <0,n>  
<35,o>
  - What is the longest chain?

---

## Open Addressing Probing

---

- Store only  $\langle K, V \rangle$  at each location in array
  - No awkward lists
  - If key is different and location is in use then go to next spot in array
    - repeat until free location found

---

# Linear Probing Example

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- If spot is occupied, go to spot+1, spot+2, ...
- Suppose
  - hashtable size is 7
  - $h(t)=t\%7$
  - add:
    - $\langle 3, A \rangle$
    - $\langle 10, B \rangle$
    - $\langle 17, C \rangle$
    - $\langle 24, Z \rangle$
    - $\langle 3, D \rangle$
    - $\langle 4, E \rangle$

---

# Probing Distance

---

- Given a hash value  $h(x)$ , linear probing generates  $h(x), h(x) + 1, h(x) + 2, \dots$ 
  - Primary clustering – the bigger the cluster gets, the faster it grows
- Quadratic probing – $h(x), h(x) + 1, h(x) + 4, h(x) + 9, \dots$ 
  - Quadratic probing leads to secondary clustering, more subtle, not as dramatic, but still systematic
- Double hashing
  - Use a second hash function to determine jumps

---

# Performance Analysis for probing

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- In the worst case, searches, insertions and removals take  $O(n)$  time
  - when all the keys collide
- The load factor  $\alpha$  affects the performance of a hash table
  - expected number of probes for an insertion with open addressing is  $\frac{1}{1 - \alpha}$
- Expected time of all operations is  $O(1)$  provided  $\alpha$  is not close to 1
  - NOTE: cheating here  $O()$  is about true worst case

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# Open Addressing vs Chaining

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- Probing is significantly faster in practice
- locality of references – much faster to access a series of elements in an array than to follow the same number of pointers in a linked list
- Efficient probing requires soft/lazy deletions – tombstoning
  - de-tombstoning

---

# In class exercise

---

- Show the final contents of the hashtable using linear probing assuming
  - table size is 13
  - $h(t) = t \% 13$
- Data: <0,a> <32,b> <39,c> <12,d>  
<14,e> <35,f> <27,g> <13,h> <15,i>  
<5,j> <12,k> <13,l> <4,m> <0,n> <35,o>
- What is the most number of steps you needed to take to find a free location?

---

# Using Hashtables

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- No worries about hashing functions, rehashing, ...
  - Someone else responsibility
- Example: who is visiting my site, and how often?
  - for instance, hackers?
  - web servers keep access logs
  - `java.util.HashMap`