$k$-Nearest Neighbor
Instance-Based Learning

Some material adapted from slides by Andrew Moore, CMU.

1-Nearest Neighbor

- One of the simplest of all machine learning classifiers
- Simple idea: label a new point the same as the closest known point
1-Nearest Neighbor

- A type of instance-based learning
  - Also known as “memory-based” learning
- Forms a Voronoi tessellation of the instance space
Distance Metrics

Different metrics can change the decision surface

\[ \text{Dist}(a, b) = (a_1 - b_1)^2 + (a_2 - b_2)^2 \]

\[ \text{Dist}(a, b) = (a_1 - b_1)^2 + (3a_2 - 3b_2)^2 \]

- Standard Euclidean distance metric:
  - Two-dimensional: \( \text{Dist}(a, b) = \sqrt{(a_1 - b_1)^2 + (a_2 - b_2)^2} \)
  - Multivariate: \( \text{Dist}(a, b) = \sqrt{\sum (a_i - b_i)^2} \)

Adapted from “Instance-Based Learning” lecture slides by Andrew Moore, CMU.
Four Aspects of an Instance-Based Learner:

1. A distance metric
2. How many nearby neighbors to look at?
3. A weighting function (optional)
4. How to fit with the local points?

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1-NN’s Four Aspects as an Instance-Based Learner:

1. A distance metric
   - Euclidian

2. How many nearby neighbors to look at?
   - One

3. A weighting function (optional)
   - Unused

4. How to fit with the local points?
   - Just predict the same output as the nearest neighbor.

Adapted from “Instance-Based Learning” lecture slides by Andrew Moore, CMU.
LONDON (Reuters) -- For centuries visitors to the renowned Ryoanji Temple garden in Kyoto, Japan have been entranced and mystified by the simple arrangement of rocks. The five sparse clusters on a rectangle of raked gravel are said to be pleasing to the eyes of the hundreds of thousands of tourists who visit the garden each year.

Scientists in Japan said on Wednesday they now believe they have discovered its mysterious appeal.

"We have uncovered the implicit structure of the Ryoanji garden's visual ground and have shown that it includes an abstract, minimalist depiction of natural scenery," said Gert Van Tonder of Kyoto University.

The researchers discovered that the empty space of the garden evokes a hidden image of a branching tree that is sensed by the unconscious mind.

"We believe that the unconscious perception of this pattern contributes to the enigmatic appeal of the garden," Van Tonder added.

He and his colleagues believe that whoever created the garden during the Muromachi era between 1333-1573 knew exactly what they were doing and placed the rocks around the tree image.

By using a concept called medial-axis transformation, the scientists showed that the hidden branched tree converges on the main area from which the garden is viewed.

The trunk leads to the prime viewing site in the ancient temple that once overlooked the garden. It is thought that abstract art may have a similar impact.

"There is a growing realisation that scientific analysis can reveal unexpected structural features hidden in controversial abstract paintings," Van Tonder said

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**k – Nearest Neighbor**

- Generalizes 1-NN to smooth away noise in the labels
- A new point is now assigned the most frequent label of its \( k \) nearest neighbors

Label it red, when \( k = 3 \)

Label it blue, when \( k = 7 \)
**k-Nearest Neighbor (k = 9)**

- **A magnificent job of noise smoothing. Three cheers for 9-nearest-neighbor. But the lack of gradients and the jerkiness isn’t good.**

- **Appalling behavior! Loses all the detail that 1-nearest neighbor would give. The tails are horrible!**

- **Fits much less of the noise, captures trends. But still, frankly, pathetic compared with linear regression.**

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